

Thermochimica Acta 366 (2001) 79-87

thermochimica acta

www.elsevier.com/locate/tca

Phase diagram of the system $Na₃AIF₆–NaF–Na₂SO₄$

V. Danielik^{*}, J. Gabová

Department of Inorganic Technology, Faculty of Chemical Technology, Slovak University of Technology, SK-812 37 Bratislava, Slovak Republic

Received 29 March 2000; received in revised form 1 July 2000; accepted 4 September 2000

Abstract

In the phase diagram of the system NaF-Na₂SO₄, a binary compound Na₃FSO₄ exists. The compound allows to divide the ternary system $Na_3AlF_6-NaF-Na_2SO_4$ into the two subsystems $Na_3AlF_6-Na_1S_4$ and $Na_3AlF_6-Na_2SO_4-Na_3FSO_4$. Experimental coordinates of the eutectic point in the subsystem Na₃AlF₆-NaF-Na₃FSO₄ are: 7.6 mole%Na₃AlF₆ + 54.6 mole% NaF + 37.8 mole% Na₂SO₄, 761°C. Experimental coordinates of the eutectic point in the subsystem Na₃AlF₆-Na₂SO₄-Na₃FSO₄ are: 4.6 mole% Na₃AlF₆ + 26.3 mole% NaF + 69.1 mole% Na₂SO₄, 733^oC.

Thermodynamic model for calculation of the system $Na_3AlF_6-Na_2SO_4$ is presented. The thermodynamic model describes well all available thermodynamic data of the system, viz. enthalpies of mixing and solid-liquid phase equilibria. \odot 2001 Elsevier Science B.V. All rights reserved.

Keywords: Cryolite; Fluoride; Phase diagram; Ternary system; Solid-liquid equilibria

1. Introduction

Sodium sulphate is often present in small amounts in the cryolite-based electrolytes used for electrowinning of aluminium. The behavior of the sulfates in the electrolyte is not well understood [1]. Investigation of thermodynamic properties of systems containing both AlF_6^{3-} and SO_4^{2-} ions may help to clarify this problem. From this point of view, calculation of the phase diagram for the system $Na₃AIF₆–NaF–Na₂SO₄$ is interesting because it contains two congruently melting compounds, viz. $Na₃AIF₆$ and $Na₃FSO₄$.

In the system $NaF-Na₂SO₄$, the congruently melting compound $Na₃FSO₄$ exists [2]. Thus, the phase diagram $Na₃AIF₆–NaF–Na₂SO₄$ can be divided into

 * Corresponding author. Fax: $+421-7-52950171$.

the two subsystems $Na₃AIF₆-NaF-Na₃FSO₄$ and $Na₃AIF₆–Na₂SO₄–Na₃FSO₄.$

The subsystem $Na₃AIF₆–NaF–Na₃FSO₄$ has been investigated by Fellner et al. [3]. The cited authors calculated the phase diagram of the system assuming a partial thermal dissociation of the compounds $Na₃AIF₆$ and $Na₃FSO₄$ during melting. However, the agreement between the experimental and calculated phase diagram was unsatisfactory.

Results on the subsystem $Na₃AIF₆–Na₂SO₄–$ $Na₃FSO₄$ have been published previously [4]. The authors calculated the phase diagram of the system using the same assumptions as in [3]. Agreement between experimental and calculated phase diagram was also unsatisfactory.

When the two experimental subsystems had been joined to the system $Na₃AIF₆–NaF–Na₂SO₄$ by transformation of composition coordinates, the obtained crystallization area of $Na₃FSO₄$ seems to be unlikely.

E-mail address: danielik@chtf.stuba.sk (V. Danielik).

^{0040-6031/01/\$ -} see front matter \odot 2001 Elsevier Science B.V. All rights reserved. PII: S 0040-6031(00)00709-7

In this paper, we will present new data in the crystallization field of $Na₃FSO₄$ (20–65 mole% NaF; 0– 20 mole% $Na₃AIF₆$ and 35-80 mole% $Na₂SO₄$) in order to clarify these discrepancies. A thermodynamic model is proposed which describes well the experimental phase diagram data.

2. Experimental

The temperatures of individual phase transitions (primary, secondary and eutectic crystallization) were determined by thermal analysis. Cooling runs of the mixtures under investigation were carried out at a rate of 1.2–2 K min^{-1}. The temperature was measured by a PtRh10-Pt thermocouple and its thermoelectric voltage was recorded at 2.5 s intervals and registered by a computer. The thermocouple was calibrated against reference melting temperatures of pure salts. The reproducibility in determination of equilibrium temperatures was about 2 K. Experimental details can be found in [5].

3. Thermodynamic model

Thermodynamic models of systems containing complex compounds are usually based on the assumptions of a partial dissociation of these compounds [2]. However, the structure of cryolite-based melts is not reliably known [6]. In the case of addition the compound Na_3FSO_4 the anion FSO_4^{3-} does not exist in solid state [7]. Hence, it probably does not exist in the liquid state either. The model presented below is independent of the structure of the melt based on [8,9].

Let us consider the system AX-BX, in which a compound exists in the solid state, where m , n denote numbers of moles of AX and BX, respectively. In the model we assume that the compound $mAX\cdot nBX$ completely dissociates under melting to the species AX and BX.

It is convenient to change composition of the compound $mAX \cdot nBX$ into compound $(AX)_p \cdot (BX)_q$ where

$$
p = \frac{m}{m+n}, \qquad q = \frac{n}{m+n} \tag{1}
$$

It is obvious that $p + q = 1$. Thus, by melting 1 mole of the compound $(AX)_{p}$ $(BX)_{q}$, which completely dissociates to AX and BX, we will get 1 mole of the melt containing species AX and BX.The molar enthalpy of fusion of $(AX)_p \cdot (BX)_q$ equals to

$$
\Delta_{\text{fus}} H_{\text{m}}^{0}[(AX)_{p} \cdot (BX)_{q}] = \frac{\Delta_{\text{fus}} H_{\text{m}}^{0}(mAX \cdot nBX)}{m+n}
$$
 (2)

The activities of AX and BX are (standard state corresponds to pure component at the temperature and pressure of the melt)

$$
a(AX) = x(AX) \cdot \gamma(AX), \qquad a(BX) = x(BX) \cdot \gamma(BX)
$$
\n(3)

Activity coefficients of AX and BX could be obtained from the molar excess Gibbs energy:

$$
RT \ln \gamma_i = \left[\frac{\partial \left(\sum n_i \Delta G_i^{\text{E}} \right)}{\partial n_i} \right]_{T, p, n_{j \neq i}} \tag{4}
$$

We may choose a new standard state in order to calculate hypothetic activity of $(AX)_{p}$ $(BX)_{q}$. The new standard state means the melt with the composition of the pure compound $(AX)_{p}(BX)_{q}$ at the temperature and the pressure of the melt.

Formally, the compound $(AX)_{p}$ $(BX)_{q}$ divides the system AX-BX into two subsystems $AX-(AX)_p$ $(BX)_q$ and $(AX)_{p}(BX)_{q}$ -BX. Then the molar Gibbs energy of a subsystem ΔG_{m}^* [i.e. AX–(AX)_p·(BX)_q] is

$$
\Delta G_{\rm m}^* = \Delta G_{\rm m} - (1 - x_i^*) \Delta G_{\rm m}^0 \tag{5}
$$

where ΔG_{m} denotes the molar Gibbs energy of the system AX-BX; x_i^* is mole fraction of a component " i " in the subsystem [i.e. mole fraction AX in the subsystem AX– $(AX)_p \cdot (BX)_q$]; ΔG_m^0 denotes the value of the molar Gibbs energy of the system AX-BX at the composition of the pure compound $(AX)_{p}(BX)_{q}$.

When we assume that the chemical potential of the compound $(AX)_{p}(BX)_{q}$ corresponding to its standard state is

$$
\mu[(AX)_p \cdot (BX)_q] = p\mu(AX) + q\mu(BX) \tag{6}
$$

then for the activity of $(AX)_{p}(BX)_{q}$ it holds

$$
a[(AX)_p(BX)_q] = x[(AX)_p(BX)_q] \cdot \gamma[(AX)_p(BX)_q]
$$

$$
= \frac{x(AX)^p \cdot x(BX)^q}{x(AX)_0^p \cdot x(BX)_q^q}
$$

$$
\times \frac{\gamma(AX)^p \cdot \gamma(BX)^q}{\gamma(AX)_0^p \cdot \gamma(BX)_0^q}
$$
(7)

where $x(i)_0$ and $y(i)_0$ are the mole fractions and activity coefficients of AX and BX in the melt with the composition of the pure compound $(AX)_{p}(BX)_{q}$, respectively.

In the binary system the composition dependence of the molar excess Gibbs energy can be described by

$$
\Delta G_{\rm m}^{\rm E} = x_1 x_2 (g_0 + g_1 x_2 + g_2 x_2^2 + g_3 x_2^3) \tag{8}
$$

When the data on the enthalpy of mixing are available (which is the case of the systems $NaF-Na_2SO_4$, $Na₃AIF₆-NaF$, we can express the molar excess Gibbs energy from the classical relationship

$$
\Delta G_{\rm m}^{\rm E} = \Delta H_{\rm m,mix} - T \Delta S_{\rm m}^{\rm E} \tag{9}
$$

where $\Delta H_{\text{m,mix}}$ and $\Delta S_{\text{m}}^{\text{E}}$ were assumed to be independent on temperature and may be described by equations

$$
\Delta H_{\text{m,mix}} = x_1 x_2 (h_0 + h_1 x_2 + h_2 x_2^2 + h_3 x_2^3) \tag{10}
$$

$$
\Delta S_{\rm m}^{\rm E} = x_1 x_2 (s_0 + s_1 x_2 + s_2 x_2^2 + s_3 x_2^3) \tag{11}
$$

In the Eqs. (9)–(12) g_i , h_i , s_i are the polynomial parameters.

In the case of the ternary system the molar excess Gibbs energy of the system can be described by the relationship

$$
\Delta G_{\rm m}^{\rm E} = \sum \Delta G_{\rm m, binary}^{\rm E} + \sum g_{ijk} x_1^i x_2^j x_3^k \tag{12}
$$

where i, j, k are integer values.

4. Results and discussion

New experimental data were obtained in the concentration range $2-10$ mole% Na₃AlF₆; 23– 61 mole% NaF and 31-73 mole% Na₂SO₄. The experimental results are summarized in Table 1. The coordinates of eutectic points were determined as follows: 4.6 mole% $Na₃AIF₆ + 26.3$ mole% NaF+ 69.1 mole% $Na₂SO₄$, 733°C and 7.6 mole% $Na₃AlF₆$ +54.6 mole% NaF + 37.8 mole% Na₂SO₄, 761 °C.

According to Fellner et al. [3] there are solid solutions of $Na₂SO₄$ in $Na₃AlF₆$ up to 80 mole% $Na₂SO₄$ in the binary system $Na₃AlF₆–Na₂SO₄$ [3]. In the composition range mentioned above no solid solutions were determined.

Phase diagram of the system $Na₃AIF₆–NaF–$ $Na₂SO₄$ was calculated using the thermodynamic model described above. Molar enthalpies and temperatures of fusion of pure components used in the calculation are listed in Table 2. The model is based on the following assumptions and approximations:

- 1. In the first step the composition co-ordinates of the system $NaF-Na_3AlF_6$ are transformed to the system $NaF-NaAlF₄$. This transformation does not reflect the real ionic composition of the melt, but it is suitable to describe the thermodynamic properties. Therefore, the calculated ternary system is NaF-NaAlF₄-Na₂SO₄.
- 2. The excess Gibbs energy $(J \text{ mol}^{-1})$ of the system NaF $-NaAIF₄$ is expressed by the equation

$$
\Delta G_{\text{m}}^{\text{E}} = x(\text{NaF})x(\text{NaAlF}_4) \{a_0 + a_1x(\text{NaAlF}_4) + a_2[x(\text{NaAlF}_4)]^2 + a_3[x(\text{NaAlF}_4)]^3\}
$$

The parameters of the above equation were determined by a non-linear regression analysis (the criterion of the least squares, confidence level 99%) using the available experimental data for the content of sodium in aluminium in contact with cryolite-based melt $[10-14]$, the vapour pressure of NaAlF₄ [15] and the solid-liquid equilibrium of NaF with the melt [16]. For the molar enthalpy of mixing of the system NaF-NaAlF₄ the data by Holm [17] and by Hong and Kleppa [18] were used. Model parameters of the molar excess Gibbs energy of the system NaF-NaAlF₄ are listed in Table 3.

Calculated and experimental data on the phase diagram and molar enthalpy of mixing of the system $NaF-NaAlF₄$ are compared in Figs. 1 and 2. It can be seen that agreement between experimental and calculated data is good.

3. The excess Gibbs energy $(J \text{ mol}^{-1})$ of the system $NaF-Na₂SO₄$ is expressed by the equation:

$$
\Delta G_{\rm m}^{\rm E} = x(\rm NaF)x(\rm Na_2SO_4)\{b_0 + b_1x(\rm Na_2SO_4) + b_2[x(\rm Na_2SO_4)]^2 + b_3[x(\rm Na_2SO_4)]^3\}
$$

For the molar enthalpy of mixing of the system $NaF-Na₂SO₄$, experimental data has been published by Hatem and Gaune-Escard [19]. Kleppa and Julsrud [20] were reported their data in the form of an equation. However, the published data

× × ۰,

Experimental temperatures of the primary crystallization ($t_{pc,exp}$), of the secondary crystallization ($t_{sc,exp}$), and the eutectic temperatures ($t_{c,exp}$) in the system $Na₃AIF₆–NaF–Na₂SO₄^a$

^a In the last column the solid phase, which crystallizes first, is presented.

are in disagreement. Data on the molar enthalpy of mixing measured by high temperature calorimetry used by Kleppa and Julsrud [20] are considered more accurate than the data measured by drop calorimetry used by Hatem and Gaune Escard

Table 2 Enthalpies and temperatures of fusion of components used for the calculation

Component	ΔH_i^{fus} (kJ mol ⁻¹)	$T_i^{\text{fus}}(K)$	Reference	
NaF	33137	1269	[21]	
Na ₃ AIF ₆	107280	1284	[1]	
Na ₂ SO ₄	23012	1157	[21]	
Na ₃ FSO ₄	69000	1060	$\lceil 2 \rceil$	

[19]. However, on the basis of data presented in this work it cannot be decided which experimental data should be preferred. Therefore, the parameters in the above equations were determined by a non-linear regression analysis (given above) for

Table 3

The parameters of the equation of molar excess Gibbs energy^a of the system $NaF-NaAlF_4$

Parameter	Calculated value			
a ₀	$-(95.6 \pm 3.5) \times 10^3 + (43.97 \pm 0.72)T$			
a ₁	$-(249 \pm 25) \times 10^3 + (202.3 \pm 3.2)T$			
a ₂	$(659 \pm 56) \times 10^3 - (502.1 \pm 6.7)T$			
a_3	$-(457 \pm 40) \times 10^3 + (347.9 \pm 5.0)T$			

^a Temperature is calculated in K.

Fig. 1. Phase diagram of the system NaF-NaAlF₄: (\bullet) data by Solheim and Sterten [16]; (\leftarrow) calculated.

each set of data [19,20]. Evaluation of the molar excess entropy of the system $NaF-Na_2SO_4$ was conducted from the solidus-liquidus equilibrium data reported by Koštenská and Malinovský [2]. Model parameters of the molar excess Gibbs energy of the system $NaF-Na_2SO_4$ are listed in Table 4. Model A uses experimental enthalpy data published by Hatem and Gaune-Escard [19]; model B uses those from the equation reported by Kleppa and Julsrud [20].

The molar enthalpy of mixing and molar excess entropy of the system $NaF-Na_2SO_4$ is given in Fig. 3. It can be seen that even the mixing data by Hatem and Gaune-Escard [19] and Kleppa and Julsrud [20] are very different, the calculated curves of solidus-liquidus equilibria according to these data are almost identical (see Fig. 4). It follows that the calculation of phase diagram is not suitable for verification of the data on enthalpy of mixing.

Fig. 2. Molar enthalpy of mixing of the system NaF-NaAlF₄: (O) data by Hong and Kleppa [18]; (\bullet) data by Holm [17]; (\leftarrow) calculated.

^a Temperature is calculated in K.

Fig. 3. Molar enthalpy of mixing and molar excess entropy of the system NaF-Na₂SO₄: (\Box) data by Hatem and Gaune-Escard [19]; (-)(1), calculated molar enthalpy of mixing based on the paper by Hatem and Gaune-Escard $[19]$; (\cdots) (1), calculated molar excess entropy based on the paper by Hatem and Gaune-Escard [19]; $(-)$ (2), equation published by Kleppa and Julsrud [20]; (\cdots) (2), calculated molar excess entropy based on the paper by Kleppa and Julsrud [20].

Fig. 4. Phase diagram of the system NaF-Na₂SO₄: (O) experimental data by Koštenská and Malinovský [2]; (--) calculated data based on the paper by Hatem and Gaune-Escard [19]; (\cdots) calculated data based on the paper by Kleppa and Julsrud [20].

4. Molar excess Gibbs energy $(J \text{ mol}^{-1})$ of the system $NaF-NaAlF_4-Na_2SO_4$ is expressed by the equation

$$
\Delta G_{\rm m}^{\rm E} = \sum A G_{\rm m, binary}^{\rm E} + d_1 x_1 x_2^2 x_3 + d_2 x_1 x_2^3 x_3^2 + d_3 x_1^2 x_2^2 x_3^2 + d_4 x_1^3 x_2 x_3 + d_5 x_1^3 x_2 x_3^2 + d_6 x_1^3 x_2^3 x_3^2
$$

where x_1 , x_2 , x_3 are mole fractions of NaF, NaAlF₄ and $Na₂SO₄$, respectively.

The molar excess Gibbs energy $(J \text{ mol}^{-1})$ of the system $NaAlF_4-Na_2SO_4$ had to be calculated from the ternary system since no data on the binary system were available. The model equation of molar excess Gibbs energy of this binary system was determined as

$$
\Delta G_{\rm m}^{\rm E} = x(\text{NaAlF}_4)x(\text{Na}_2\text{SO}_4)\{c_0+c_2[x(\text{Na}_2\text{SO}_4)]^2\\ + c_3[x(\text{Na}_2\text{SO}_4)]^3\}
$$

The parameters of above equations were determined by a non-linear regression analysis (given above) using experimental data on solidus-liquidus equilibria of the system $Na₃AIF₆-NaF Na₂SO₄$ ([3,4], this work) which were transformated to the system $NaF-NaAlF_4-Na_2SO_4$. The parameters of the above equations and probable inaccuracy of the system NaF-NaAlF₄-Na₂SO₄

Table 5

The parameters of the molar excess Gibbs energy^a and probable inaccuracy of the system NaF-NaAlF₄-Na₂SO₄ for both models^b

Parameter	Model A	Model B		
c_0	$-(24.1 \pm 1.8) \times 10^3$			
c ₂	0	$(58 \pm 11) \times 10^3$		
c ₃	2950 ± 690	$-(78.6 \pm 7.8) \times 10^{3}$		
d ₁	$(157 \pm 20) \times 10^{3}$	0		
d_2	$\mathbf{\Omega}$	$(5.81 \pm 0.21) \times 10^{6}$		
d_3	0	$-(3.14 \pm 0.13) \times 10^{6}$		
d_4	$-(173 \pm 11) \times 10^3$	0		
d_{5}	0	$(275 \pm 19) \times 10^3$		
d ₆	$(2.86 \pm 0.30) \times 10^6$	0		
σ_1 (°C)	11.6	13.7		
σ_2 (°C)	6.7	7.4		

^a Temperature is calculated in K.

 b_{σ_1} denotes the probable inaccuracy of the all experimental data on the ternary system ([3,4], this work); σ_2 denotes the probable inaccuracy of the data published in this work.

are listed in Table 5 for both models. It can be seen that the agreement between calculated and the experimental data from this work is better than the agreement between calculated and previously published data [3,4]. The crystallization area of $Na₃FSO₄$ seems to be unlikely according to the previously published experimental data [3,4].

Comparison of the experimental and calculated data is shown in Figs. 5 and 6. Experimental and

Fig. 5. Phase diagram of the system Na₃AlF₆–Na₂SO₄: (\bigcirc) experimental [3]; (—) calculated (both models based on the papers by Hatem and Gaune-Escard [19] and Kleppa and Julsrud [20] give identical values).

Fig. 6. Phase diagram of the system $Na_3AlF_6-Na_7SO_4$: (\cdots) experimental (this work); (\cdots) calculated curves based on the paper by Hatem and Gaune-Escard [19]; (- - -) calculated curves based on the paper by Kleppa and Julsrud [20]; isothermes are calculated according to the paper published by Hatem and Gaune-Escard [19].

Table 6 Experimental and calculated ternary eutectic points

	Experimental		Model A		Model B	
	e_1	e ₂	e_1	e ₂	e ₁	e ₂
$X(Na_3AlF_6)$	0.046	0.076	0.041	0.077	0.033	0.056
x(NaF)	0.263	0.546	0.251	0.565	0.236	0.578
$X(Na_2SO_4)$	0.691	0.378	0.708	0.358	0.731	0.366
t (°C)	733	761	729.8	756.6	737.5	777.3

calculated ternary eutectic points are listed in Table 6. It can be seen that the model using the molar enthalpy of mixing by Hatem and Gaune-Escard [19] describes experimental data better than the model using for the molar enthalpy of mixing the equation by Kleppa and Julsrud [20]. However, the difference between these two models is too small to allow to make any further conclusions. Both models describe all experimental data $([3,4],$ this work) on solid-liquid equilibria well within the range of experimental error.

Acknowledgements

This work was supported by the Research grant no. 1/6250/99 of the Slovak Grant Agency (VEGA 1/6250/99).

References

- [1] K. Grjotheim, C. Krohn, M. Malinovský, K. Matiašovský, J. Thonstad, Aluminium Electrolysis — Fundamentals of the Hall — Héroult Process, 2nd Edition, Aluminium — Verlag, Düsseldorf, 1982.
- [2] I. Koštenská, M. Malinovský, Chem. Zvesti 36 (1982) 159.
- [3] P. Fellner, J. Gabová, V. Danielik, Thermochim. Acta 242 (1994) 243.
- [4] P. Fellner, J. Gabová, V. Danielik, M. Láska, Chem. Papers 47 (1993) 215.
- [5] P. Fellner, J. Gabová, Thermochim. Acta 206 (1992) 321.
- [6] B. Gilbert, E. Robert, E. Tixhon, J.E. Olsen, T. Østvold, Inorg. Chem. 35 (1996) 4198.
- [7] A. Pabst, Am. Mineral AMMIA 58 (1973) 116.
- [8] T. Foosnes, T. Østvold, H. Øye, Acta Chem. Scand. A32 (1978) 973.
- [9] W.Ch. Bale, A.D. Pelton, Met. Trans. B14 (1983) 77.
- [10] W.H. Tingle, J. Petit, W.B. Frank, Aluminium 57 (1981) 286.
- [11] R.D. Peterson, A.T. Tabereaux, Light Met. (1986) 491.
- [12] V. Danielik, P. Fellner, Chem. Papers 52 (1998) 195.
- [13] E.W. Dewing, M.J. Gilbert, Light Met. (1980) 221.
- [14] P. Fellner, Ž. Lubyová, Chem. Papers 40 (1986) 145.
- [15] J. Guzman, K. Grjotheim, T. Østvold, Light Met. (1986) 425.
- [16] A. Solheim, Å. Sterten, in: Proceedings of the Ninth International Symposium On Light Metals Production, Tromsø-Trondheim, Norway, 19-21 August 1997, p. 225.
- [17] J.L. Holm, Thermodynamic properties of molten cryolite and other fluoride mixtures, Thesis, Institute of Inorganic Chemistry, NTH, Trondheim, Norway, 1971.
- [18] K.C. Hong, O.J. Kleppa, High Temp. Sci. 8 (1976) 299.
- [19] G. Hatem, M. Gaune-Escard, J. Phys. Chem. 86 (1982) 3039.
- [20] O.J. Kleppa, S. Julsrud, Acta Chem. Scand. A34 (1980) 655.
- [21] D.R. Stull, H. Prophet, JANAF Thermochemical Tables, 2nd Edition, Nat. Bur. Stand. (USA), Coden NSRDA, 1971.